

A strategy for speed Dating

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ABSTRACT

Online dating is a growing industry with recent quarterly profits well in excess of millions. The goal of PIZZAZ.com is to break into this industry that using the power of statistics to optimally match couples.

In order to attain this target, we will use a fictional dataset speeding dataset to generate models to test feasibility of using statistics to match couples.

INTRODUCTION

In this paper, the author acknowledge that some of the figures are rather small. It is suggested that a reader might print the paper and download the PDF.

This paper is divided into the following _4_ main sections:

- 1) Brief introduction for our speed dating data
- 2) Some Basic Hypothesis
 - 2.1) Impact of race
 - 2.2) Impact of age range
 - 2.3) the correlation between like ratings and other independent variables
- 3) Building a model
 - 3.1) Strategy to build the model for male (dependent variable)
 - 3.2) Regression diagnostics for the candidate model for male (dependent variable)
 - 3.3) Collinearity test for the candidate model for male (dependent variable)
 - 3.4) Logistic regression model for male (dependent variable)
 - 3.5) **All the process repeated above for female**
- 4) Conclusion

1) BRIEF INTRODUCTION FOR OUR SPEED DATING DATA

The chart in Figure 1 illustrates The target (Y) is (a numerical), indicating how much do you like this person

For each male dater, 9 input (X) variables were recorded;

A dater's opinion of the person, as indicated by the like variable. based on the attractiveness, sincerity, Intelligence, Fun, ambitious And shared interest of their partner

Name	model role	level	description
LikeF	target 1	num	how much do you like this female(1=don't like at all, 10=like a lot)
LikeM	target 2	num	how much do you like this male(1=don't like at all, 11=like a lot)
AgeF	input	num	age for female
AgeM	input	num	age for male
AmbitiousF	input	num	rate ambition of female on a scale of 1 - 10 (1=awful,10=great)
AmbitiousM	input	num	rate ambition of male on a scale of 1 - 10 (1=awful,11=great)
AttractiveF	input	num	rate attractiveness of female on a scale of 1-10(1=awful, 10=great)
AttractiveM	input	num	rate attractiveness of male on a scale of 1-10(1=awful, 11=great)
DecisionF	input	num	female's decision: 1=yes(want to see the date again); 0=No(do not want to see again)
DecisionM	input	num	male's decision: 1=yes(want to see the date again); 1=No(do not want to see again)
FunF	input	num	rate how fun female is on a scale of 1-10 (1=awful, 10=great)
FunM	input	num	rate how fun male is on a scale of 1-10 (1=awful, 10=great)
IntelligentF	input	num	rate how intelligent female is on a scale of 1-10 (1=awful, 10=great)
IntelligentM	input	num	rate how intelligent male is on a scale of 1-10 (1=awful, 10=great)
PartnerYesF	input	num	how probable do you think it is that the female will say "yes" for you
PartnerYesM	input	num	how probable do you think it is that the male will say "yes" for you
RaceF	input	char	race for female (Caucasian, Asian, Black, Latino, or Other)
RaceM	input	char	race for male (Caucasian, Asian, Black, Latino, or Other)
SharedInterestsF	input	num	rate the extent to which you share intests with partner on a scale of 1-10
SharedInterestsM	input	num	rate the extent to which you share intests with partner on a scale of 1-10
SincereF	input	num	rate sincerity of female on a scale of 1-10
SincereM	input	num	rate sincerity of male on a scale of 1-11

Figure 1

2) SOME BASIC HYPOTHESIS

2.1) IMPACT OF RACE

Frequency Percent Row Pct Col Pct	Table of RACEM by RaceF						
	RaceM	RaceF					Total
		Asian	Black	Caucasian	Latino	Other	
Asian	9 4.97 25.00 20.93	1 0.55 2.78 12.50	22 12.15 61.11 21.36	3 1.66 8.33 20.00	1 0.55 2.78 8.33	36 19.89	
Black	3 1.66 42.86 6.98	0 0.00 0.00 0.00	2 1.10 28.57 1.94	1 0.55 14.29 6.67	1 0.55 14.29 8.33	7 3.87	
Caucasian	21 11.60 18.92 48.84	6 3.31 5.41 75.00	69 38.12 62.16 66.99	8 4.42 7.21 53.33	7 3.87 6.31 8.33	111 61.33	
Latino	3 1.66 27.27 6.98	1 0.55 9.09 12.50	4 2.21 36.36 3.88	1 0.55 9.09 6.67	2 1.10 18.18 16.67	11 6.08	
Other	7 3.87 43.75 16.28	0 0.00 0.00 0.00	6 3.31 37.50 5.83	2 1.10 12.50 13.33	1 0.55 6.25 8.33	16 8.84	
Total	43 23.76	8 4.42	103 56.91	15 8.29	12 6.63	181 100.00	

Frequency Missing = 3

In total, there are 80 couples have the same race

Figure 2

The first test I will perform the effect of same race on the Like variable. From a cross-tabulation we see there are 80 same-race couples (Figure 2). A dummy binary variable was created with the value 1 for same race, 0 for different; our model then looks like:

H0: there is no significant relationship between race and like variable;

Model: $\text{like} = \beta_0 + \beta_1 * \text{race}$;

so, we see for man: the extent to like this person will be less than 0.015 point if they are the same race, comparing to the diff race;

but the P value is 0.9525; so there is no significantly diff on the extent of like whether this lady is the same race or not;

Parameter	Estimate	Standard Error	t Value	Pr > t
Intercept	6.647058824	0.17730216	37.49	<.0001
race	-0.015808824	0.26742668	-0.06	0.9529

for woman: the extent to like this person with same race will be greater than 0.1475 point, comparing to the different race; but the P value is 0.5479;

so there is no significantly diff on the extent of like whether this man is the same race or not

Parameter	Estimate	Standard Error	t Value	Pr > t
Intercept	6.315000000	0.17501445	36.08	<.0001
race	0.147500000	0.26252167	0.56	0.5749

2.2) THE IMPACT OF AGE RANGE

Parameter	Estimate	Standard Error	t Value	Pr > t
Intercept	6.838235294	0.21634889	31.61	<.0001
age	-0.316305470	0.27336188	-1.16	0.2488

whether partner are the same age range (the same age range is defined by being within 2 years of one another)

H0: there is no significant relationship between age range and the extent of like

model : $\text{like} = \beta_0 + \beta_1 * \text{age}$; if they are the same age range, age will be 0, if they are not the same age range, age=1

therefore , we see for man: the extent to like this person without the same age range will be less than 0.316, comparing to the same age range;

but the P value is 0.2488; so there is no significantly diff on the extent of like whether this lady is the same age range or not

Parameter	Estimate	Standard Error	t Value	Pr > t
Intercept	6.477611940	0.21380665	30.30	<.0001
age	-0.154603091	0.26984739	-0.57	0.5674

for woman: the extent to like this person will be greater than 0.1546 point if they are not the same age range, comparing to the same age range;

but the P value is 0.5674; so there is no significantly diff on the extent of like whether this man is the same age range or not

age	Frequency	Percent	Cumulative Frequency	Cumulative Percent
0	69	37.50	69	37.50
1	115	62.50	184	100.00

I create a new variable-age: when $0 \leq \text{agem} - \text{agef} \leq 2$ or $0 \leq \text{agef} - \text{agem} \leq 2$. then age is 0; otherwise;
 So , we see there are 69 couples are in the same age range in our data

2.3) THE CORRELATION BETWEEN LIKE RATINGS AND OTHER INDEPENDENT VARIABLES

First, from the big visual:

We see: For men, they prefer to like younger woman with humor , and women who like to share interest and hobbies with partner, and they are more likely to predict this woman will say yes to them.

	LikeM	AgeF	AttractiveF	AmbitiousF	FunF	IntelligentF	SharedInterestsF	SincereF	PartnerYesF
LikeM	1.00000	-0.13466	0.02966	0.04203	0.24317	0.08799	0.22337	0.11661	0.18701
	182	0.0707 181	0.6918 181	0.5819 174	0.0011 178	0.2388 181	0.0043 162	0.1180 181	0.0119 180

For woman, we see: they prefer to like men who are intelligent , more ambitious and more sincere, and they are more likely to predict this man will say yes to them

	LikeF	AgeM	AttractiveM	AmbitiousM	FunM	IntelligentM	SharedInterestsM	SincereM	PartnerYesM
LikeF	1.00000	-0.06556	0.10564	0.16631	0.11490	0.17726	0.13749	0.22824	0.15141
	180	0.3860 177	0.1605 178	0.0312 168	0.1289 176	0.0189 175	0.0792 164	0.0022 178	0.0442 177

3) BUILDING A MODEL

3.1) STRATEGY TO BUILD THE MODEL FOR MALE (DEPENDENT VARIABLE)

First , I will focus on analyzing the man's like extent and build the model looks like :

$$\text{likeM} \sim \beta_0 + \beta_1 * X_{1.f} + \beta_2 * X_{2.f} + \dots + \beta_j * X_{i.f}$$

where X_i are a series of variables.

The following are some common criteria that we use to rank a model

- 1) Multiple R^2
- 2) MSE(P)
- 3) Mallows $C_p = \frac{MSE(p)}{MSE(K)} [n - p] - n + 2p$

For the Mallows: the C_p statistic is often used as a stopping rule for various forms of regression

C_p has expectation nearly equal to P

we find the point where C_p is less than or equal to p .

If $C_p < 0$ in extreme cases. It is suggested that one should choose a subset that has C_p approaching P ,

All possible models

We will consider all the conditions when we build the maximum model, single independent variable , all second order variables: then we use SAS to select the better model with all possible selection;

Number in Model	R-Square	C(p)	MSE	Variables in Model
2	0.1174	1.9649	2.57490	AgeF AF1
2	0.1174	1.9730	2.57504	PartnerYesF2 FS5
2	0.1170	2.0290	2.57601	FunF2 SP7

So , we select 2 variables: partneryesF² and FS5 kept in our model based on the all possible selection method; Among the FS5 means interaction between funf and sinceref;

Then I will fix the model, because automated model building programs often will include higher order polynomial terms or interactions without including base terms;

Therefore, I add the base term in my model,

$Y \sim \beta_0 + \beta_1 * \text{funf} + \beta_2 * \text{partneryesF} + \beta_3 * \text{sinceref} + \beta_3 * \text{funf} * \text{sinceref} + \beta_4 * \text{partneryesF}^2$, then ask SAS to run the regression.

After adjusting the model , the only variable I want to keep in the model is funf, which can significantly predict the dependent variable.

$Y \sim 5.2766 + 0.2088 * \text{funf}$

Parameter	Estimate	Standard Error	t Value	Pr > t
Intercept	5.276567072	0.43175691	12.22	<.0001
FunF	0.208778685	0.06277594	3.33	0.0011

We see the coefficient estimate of funf (slope) is 0.2088, which means one unit increase in funf, the extent of like will increased by 0.2088 for man on average. We see the R square is 0.059, which means we just have 5.9% variability of the extent of likem can be explained by these X variables for our model funf;

R-Square	Coeff Var	Root MSE	LikeM Mean
0.059129	25.50191	1.695590	6.648876

Stepwise forward selection

Parameter	Estimate	Standard Error	t Value	Pr > t
Intercept	11.41758409	2.18083826	5.24	<.0001
AgeF	-0.08019185	0.03464985	-2.31	0.0219
FunF	-0.55229984	0.30532461	-1.81	0.0723
IntelligentF	-0.62071382	0.23867101	-2.60	0.0101
FunF*IntelligentF	0.09884746	0.03696605	2.67	0.0082
racef1	0.17965034	0.53594246	0.34	0.7379
racef2	-0.22096039	0.74328824	-0.30	0.7666
racef3	0.75742700	0.49556538	1.53	0.1283
racef4	1.52509537	0.64363444	2.37	0.0190

From the estimate coefficient table, we see the extent of likem for racef4 (latino) higher 1.53 than others on average, the extent of likem for Caucasian is higher 0.76 than other, the extent of likem for black is lower 0.22 than other, the extent of likem for Asian is higher 0.18 than other on average ;

R-Square	Coeff Var	Root MSE	LikeM Mean
0.175900	24.40903	1.617792	6.627841

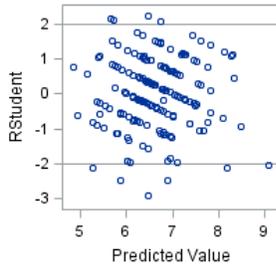
In this model, We see the R square is 17.60%, which means we just have 17.60% variability of the extent of likem can be explained by these X variables for our model agef, funf , intelligentf and racef ;

So , comparing r square between these two models, I will select the latter one would be better , because the variability of dependent variable can by explained more by our independent variables

3.2) REGRESSION DIAGNOSTICS FOR THE CANDIDATE MODEL FOR MALE (DEPENDENT VARIABLE)

Regression diagnostics are statistical techniques designed to detect conditions which can lead to inaccurate or invalid regression results.

Fit Diagnostics for LikeM



From the plot of the studentized or jackknife residual versus predicted values, there are some outliers with residuals above or lower than -2; It means those observations are further away from our predicted line;

I suggest go back to check those observations

Studentized or jackknife residual means we test the relationship between the residual and predicted value after we removing the *i*th observation out.

Then I want to check whether outliers exists with cook's distance; leverage statistics and jackknife residual

Based on the rules, we know the cutoff value of cook's distance is 1, the leverage critical value is $h > 2(K+1)/n = 2*(8+1)/176 = 0.102$;

The jackknife residual cutoff value is 2; So , we see these two observations are outliers

Obs	LikeM	jackknife	cooks	leverage
128	6	-2.05654	0.062465	0.11933
148	5	-2.12224	0.065579	0.11801

Test assumptions

- 1) Normality.
- 2) Homogeneity.
- 3) Linearity (Errors have mean of zero)
- 4) Independence

Tests for Normality				
Test	Statistic			p Value
Shapiro-Wilk	W	0.989221	Pr < W	0.2026
Kolmogorov-Smirnov	D	0.043174	Pr > D	>0.1500
Cramer-von Mises	W-Sq	0.051852	Pr > W-Sq	>0.2500
Anderson-Darling	A-Sq	0.431194	Pr > A-Sq	>0.2500

Our hypothesis:

H0- it follows the normal distribution;

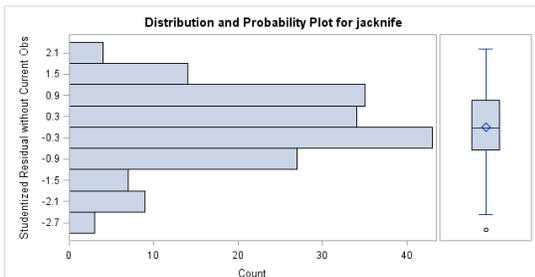
Ha- it violate the normal distribution

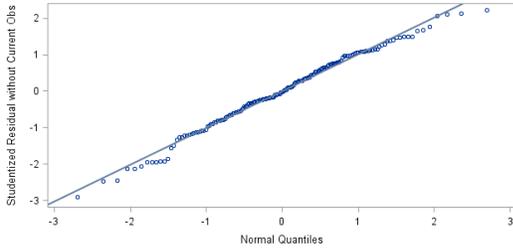
We see the Kolmogorov-Smirnov indicator, the p value is >0.15;

So I will fail to reject the H0. It means it meet the normality assumption for data

From the distribution and probability plot, the pattern follow the normality shape;

But one spot has too small and negative residual

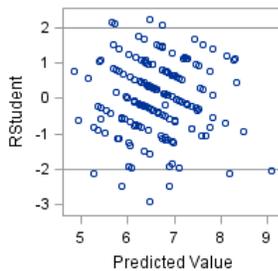




From the Q-Q plot, we see there are several spots spread a little bit further from the linear line

2) Homogeneity

Fit Diagnostics for LikeM



From the pattern, I cannot see there is an obvious funnel shape exists as the predicted value increase, and those spots do not spread out too much from each other;

Therefore, It seems satisfy the homogeneity assumption from this plot.

3) Linearity (Errors have mean of zero)

For the linearity, we observe if these plots are curvature in the plot;

It means if a repeated pattern of y value falling above and below the

Linear $y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \dots + \beta_j X_j$; then its residual pattern will be a Repeated pattern falling above and below $y=0$

In this case, it does not like curvature pattern, so I think it does not violate linearity;

4) Independence

From the plot, it seems no obvious evidence to show there is correlation

Between each observations. So I think it does not violate the independence

3.3) COLLINEARITY TEST FOR THE CANDIDATE MODEL FOR MALE (DEPENDENT VARIABLE)

The next test is to test for collinearity. In statistics, collinearity is a phenomenon in which one predictor variable in a multiple regression model can be linearly predicted from the others with a substantial degree of accuracy. I will focus on collinearity since this is often a major problem in polynomial regression. Since all our variables are functions of other variables.

Two criterions to test collinearity: condition number and variance inflation factor

(VIF is an index that measures how much the variance of estimated regression coefficient is increased because of collinearity).

In this case, we see the condition number is less than 30 but we have very high Variance Inflation Factors that easily exceed 10.

Because of VIF exceeds 10, it means the collinearity exists. Therefore, I will fix the collinearity with center the X variables

Parameter Estimates						
Variable	DF	Parameter Estimate	Standard Error	t Value	Pr > t	Variance Inflation
Intercept	1	8.01840	0.98738	8.12	<.0001	0
AgeF	1	-0.08019	0.03465	-2.31	0.0219	1.03844
FunF	1	0.22958	0.06554	3.50	0.0006	1.19258
IntelligentF	1	0.02970	0.09840	0.30	0.7631	1.29373
FI4_fix	1	0.09885	0.03697	2.67	0.0082	1.09686
racef1	1	0.17965	0.53594	0.34	0.7379	3.50940
racef2	1	-0.22096	0.74329	-0.30	0.7666	1.61197
racef3	1	0.75743	0.49557	1.53	0.1283	4.05189
racef4	1	1.52510	0.64363	2.37	0.0190	2.03969

Collinearity Diagnostics (Intercept adjusted)										
Number	Eigenvalue	Condition Index	Proportion of Variation							
			AgeF	FunF	IntelligentF	FI4_fix	racef1	racef2	racef3	racef4
1	1.86636	1.00000	0.02042	0.00447	0.05108	0.04201	0.04726	0.00089628	0.05144	0.01047
2	1.45538	1.13243	0.01392	0.21821	0.14891	0.00327	0.00000263	0.08812	0.01543	0.00569
3	1.17683	1.25933	0.09286	0.01070	0.00095845	0.04611	0.06085	0.00056772	0.00056476	0.23140
4	1.04367	1.33726	0.05879	0.00007693	0.05522	0.28639	0.01769	0.23971	0.00206	0.02677
5	0.95318	1.39930	0.49350	0.04679	0.00169	0.16228	0.00199	0.03277	0.02100	0.07635
6	0.85111	1.48083	0.29968	0.21846	0.00310	0.23491	0.00165	0.18336	0.00021399	0.01928
7	0.53885	1.86108	0.01447	0.49956	0.73825	0.22380	0.00843	0.00043655	0.00254	0.00188
8	0.11463	4.03508	0.00636	0.00173	0.00079017	0.00121	0.06213	0.45413	0.90674	0.62817

Now, we see all VIF are less than 10, and condition number is less than 30;

After fixing the collinearity, this is our final model shown on the below:

Parameter	Estimate	Standard Error	t Value	Pr > t
Intercept	8.018397576	0.98738013	8.12	<.0001
AgeF	-0.080191849	0.03464985	-2.31	0.0219
FunF	0.229583562	0.06553631	3.50	0.0006
IntelligentF	0.029702453	0.09839666	0.30	0.7631
FI4_fix	0.098847459	0.03696605	2.67	0.0082
racef1	0.179650345	0.53594246	0.34	0.7379
racef2	-0.220960388	0.74328824	-0.30	0.7666
racef3	0.757427000	0.49556538	1.53	0.1283
racef4	1.525095365	0.64363444	2.37	0.0190

From the estimate coefficient table, we see the extent of like for racef4 (latino) higher 1.53 than others on average, the extent of like for Caucasian is higher 0.76 than other, the extent of like for black is lower 0.22 than other, the extent of like for Asian is higher 0.18 than other on average ;

Each unit increase in the age of female, the extent of like will be decreased by 0.08 on average for man;

Each unit increase in the funf of female, the extent of like will be increased by 0.23 on average for man;

Each unit increase in the intelligent of female, the extent of like will be increased by 0.03 on average for man;

There is interaction between funf and intelligencef, which can add a significant prediction in our model

3.4) LOGISTIC REGRESSION MODEL FOR MALE (DEPENDENT VARIABLE)

Finally, I will use logistic regression model to test the relationship between man's decision and man's like extent; from the output table above, we know Wald χ^2 is 35.53. is substantially greater than $df=1$, so we may reject the H_0 ; P-value $<0.0001 < 0.05$ (alpha value), so I will reject the H_0 .

Conclusion : We are convincing evidence for significant effect due to the extent of like for male.

Probability modeled is DecisionM=1.

Analysis of Maximum Likelihood Estimates					
Parameter	DF	Estimate	Standard Error	Wald Chi-Square	Pr > ChiSq
Intercept	1	-5.1091	0.8921	32.8017	<.0001
LikeM	1	0.7815	0.1311	35.5340	<.0001

$\pi_i = P(Y_i=1) = P(\text{the probability of decision } M=\text{yes for female } i \text{ in measure of the extent of like})$

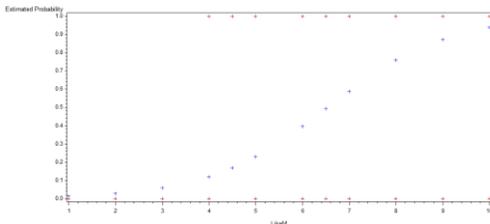
$E(\ln(\pi_i/(1-\pi_i))) = \beta_0 + \beta_1 X_i$ (β_0 : population intercept; β_1 : population slope)

Odds Ratio Estimates			
Effect	Point Estimate	95% Wald Confidence Limits	
LikeM	2.185	1.690	2.825

We see the odds ratio is 2.185; means one unit change in odds favor of “decision=yes” for each one unit increase in the value of LikeM

we can be 95% confident that the OR associated with a one unit increase in likeM falls between 1.690 and 2.825; This is a set of plausible values for the population odds ratio associated a one-unit increase likeM, comparing to the relative odds.

Note: that 1 is not in the interval, it means that is not a plausible for the odds in favor of decision =yes associated with a one-unit increase to be equal.



We see the estimated probability of decisionM increased as the likeM goes up; after the likeM point above 8, the trend of increase becomes slower and a bit flatter from this curve pattern.

3.5) ALL THE PROCESS REPEATED ABOVE FOR FEMALE

I build model with these two methods: Stepwise forward selection and All possible models:

then , I compare r square between these two models, I will select the latter one would be better-all possible models , because the variability of dependent variable can by explained more by our independent variables.

Tests for Normality				
Test	Statistic	p Value		
Shapiro-Wilk	W	0.974697	Pr < W	0.0044
Kolmogorov-Smirnov	D	0.097693	Pr > D	<0.0100
Cramer-von Mises	W-Sq	0.238718	Pr > W-Sq	<0.0050
Anderson-Darling	A-Sq	1.469066	Pr > A-Sq	<0.0050

Our hypothesis:

H0- it follows the normal distribution;

Ha- it violate the normal distribution

We see the Kolmogorov-Smirnov indicator, the p value is <0.01;

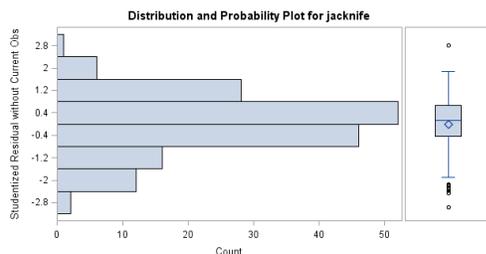
So I will reject the H0. It means it violate the normality assumption for data

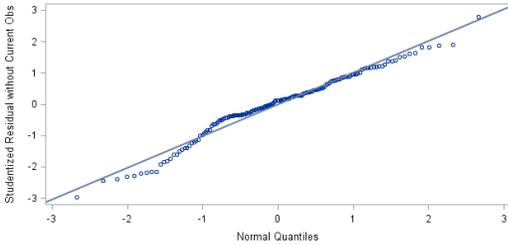
We can try to fix the normality with square transform

From the distribution and probability plot, the pattern follow the normality shape;

But some spots has too small and negative residual

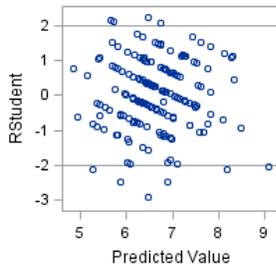
One spot is too high and positive





From the Q-Q plot, we see there are several spots spread a little bit further from the linear line

Fit Diagnostics for LikeM



From the plot of the studentized or jackknife residual versus predicted values, there are some outliers with residuals above or lower than -2; It means those observations are further away from our predicted line;

I suggest go back to check those observations

Based on the rules, we know the cutoff value of cook's distance is 1, the leverage critical value is $h > 2(K+1)/n = 2*(6+1)/163 = 0.086$;

The jackknife residual cutoff value is 2; we see there are almost 45 observations have problem either violate three of them (cooks, leverage, jackknife) one observations are outliers

we see there are almost 45 observations have problem either violate three of them (cooks, leverage, jackknife) one observations are outliers

and the same conclusion with male test with other three assumptions (homogeneity, independence and linearity)

Parameter	Estimate	Standard Error	t Value	Pr > t
Intercept	2.199067308	0.97492089	2.26	0.0255
AgeM	0.222762931	0.10142487	2.20	0.0295
ageM2	-0.022751719	0.00816272	-2.79	0.0060
AttractiveM	0.110381837	0.14313205	0.77	0.4418
AA1_fix	-0.051144626	0.02102493	-2.43	0.0161
AmbitiousM	0.192417223	0.09558670	2.01	0.0458
SincereM	0.322095848	0.09445177	3.41	0.0008

Each unit increase in the age of male, the extent of like will be increased by 0.22 on average for female;

Each unit increase in the attractive of male, the extent of like will be increased by 0.11 on average for female;

Each unit increase in the ambitious of male, the extent of like will be increased by 0.19 on average for female;

Each unit increase in the sincere of male, the extent of like will be increased by 0.322 on average for female;

There is interaction between age and attractive, which can add a significant prediction in our model

4) CONCLUSION

In this paper, we know the PIZZAZ.com get people together using statistics. The author hopes that this paper, by showing the process of how to build models and test our models in statistics.